A Steady-State Thermal Gradient Generator for Material Characterization Using an Induction Heating System

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Abstract—Mobility/Diffusion of ions can occur mainly in two situations. The first one when a potential difference is applied to electrodes of an electrochemical device as in batteries for instance (i.e., charge/discharge). In the second one, the diffusion process is driven by the thermal gradient existing within the material. This paper deals with the design of a controlled Thermal Gradient Generator (TGG) which opens the way to thoroughly study the effect of temperature difference on the chemical diffusion and mechanical resistance of shaped samples (e.g., a pellet, a rod). This TGG uses a combination of two susceptors involving the control of their respective temperatures. One is controlled by adjusting the power of a high frequency generator which supplies an induction heating coil. The other is controlled, mainly, by the displacement of the sample/susceptors set through this same coil, with a motorized stage. The operation and control parameters are defined within a dedicated user-friendly software application. During the whole experiment, the two temperatures can be varied while the inner thermal gradient of the sample is kept constant, as long as these temperatures are high enough.

Index Terms— Computerized instrumentation, Eddy currents, Induction heating, Materials characterization, Nondestructive testing, Programmable control, Thermal gradient.

I. INTRODUCTION

THERMAL gradient devices are useful tools to study material properties such as chemical diffusion, thermal conductivity, temperature resistance, ageing, etc. The purpose of the experimental device described in this paper is to apply a controlled thermal gradient to solid samples (a few millimeters thick and about 1 cm² as cross-section) at high temperatures (up to 1000°C and beyond).

In our laboratory team, the studied samples were typically ceramics that undergo ionic diffusion and exsolution when heated up. After applying a thermal gradient across a sample in a nondestructive way, the final goal was to study the microstructures generated by the gradient on and inside the

ceramic through characterization techniques such as X-ray diffraction, SEM (Scanning Electron Microscope) or FIB-SIMS (Focused Ion Beam-Secondary Ion Mass Spectrometry).

More generally, the TGG presented here can be used to apply any temperature/time controlled gradient at moderate to high temperature between opposite faces of any type of solid insulators or semiconductors, may them be inorganic or polymers. For instance, this device would be suitable for the study of ionic thermomigration in solids (e.g. in memristors, as in Shin et al.[1]) or for the optimization of the thermal treatment of thin films, as in Metting et al.[2] (these are recent studies using more loosely controlled or conventional heating systems). The current TGG is designed to operate in air, but would perform in controlled atmospheres or vacuum too. It allows nondestructive testing.

The main concern of the study is to validate the use of an induction heating system to automatically control and stabilize both the temperature on one side of the sample (e.g., the lower face) and the temperature differential with respect to the other side of the sample, thus allowing a steady-state thermal gradient. This controlled gradient at high temperatures constitutes the novelty of this work. Heating has to be located on small surfaces and temperatures must be measured on both sides. The temperatures of both faces must be as homogeneous as possible in order to have a uniform gradient throughout the section of the sample.

Bober et al. [3] introduced an induction heating system which is built in a high-vacuum, water-cooled recipient. This setup is well suited to higher temperatures, such as 2577°C (2850K), but the gradient is adjusted manually, without an automatic control. Furthermore, the system is more expensive.

A patented system is described by Pontillon et al. [4]. It consists in a *radial* (as opposed to *axial* in our case) gradient at temperatures up to 2000°C, but it allows a single temperature set point (along the axis of the cylindrical sample). External temperature is fixed by choice of the insulator (depending on its nature and geometry), and chosen by simulation at a temperature of 350°C +/-50°C, without any attempt of automatic control.

A paper by Shihab et al. [5] describes a heating system by pulsed laser excitation, which can be used only on thin layers (typically 50 nm thick) of magnetic materials showing a hysteresis cycle, in order to get a thermal differential (ΔT) of a dozen degrees induced by the laser spot.

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Another patent application, from Obbard et al. [6], describes a device which can establish a thermal gradient within living tissue or an ice core. Two heat sinks are used, each maintained by a control mechanism at a different temperature. Each heat sink is in contact with a thermal conductor, the two conductors being set on two opposite faces of the sample. Thus, an axial thermal gradient is maintained within the sample. However, the use of heat sinks limits applications to temperatures below room temperature.

The solution adopted in our device consists in a single induction coil heating up two susceptors, one on each sample face. Susceptors can be the same if the sample is thick enough to induce a large enough thermal gradient when shifted above or below the coil center, or have different thicknesses in order to increase the gradient. A typical chosen configuration is an upper susceptor with double thickness relative to the lower one, e.g. 300 and 150 μm , respectively.

The temperature of the lower face and the temperature differential ΔT (therefore, the temperature gradient) are regulated by two independent control loops. Compared to a heating system with two heating resistors, our solution has the following advantages:

- 1) it avoids thermal bridges which inevitably degrade homogeneity in temperatures of the two susceptors (as there are no wires connected to effectors and which could sink-out heat at contact points or contact surfaces).
- 2) it makes it possible to simulate quenching or quasi-quenching more efficiently (with resistors, the thermal bridges would slow down the cooling of the susceptors),
- 3) it is more suitable for thermal cycling and fatigue investigations since it allows higher temperature rise times, as explained by Liu [7].
- 4) Finally, our solution is much less expensive than two heating systems, because even with heating resistors, the two heating systems would have to be controlled systems that are indeed the most expensive part in such a device.

This article is organized as follows. We first study a manual procedure of the proposed TGG and its preliminary calibration (Section II). Then, the automatic control of the TGG is justified and presented in Section III. Section IV introduces the control software and equipment. This is completed by a validation Section V, with some results. Finally, a conclusion is drawn and some prospects are proposed in Section VI.

II. MANUAL TGG OPERATION

Lets T_h and T_l be the stabilized temperatures of the upper (higher) and lower susceptors, respectively. Let P be the mass power dissipated by eddy currents in a sheet/pellet (induced from an induction coil, see Figure 1).

Under some conditions (mainly, uniform material, without skin effect), as explained by Nickelson[8], P is given by:

$$P = \frac{\pi^2 B^2 d^2 f^2}{6 \rho D}, \quad (1)$$

where,

P is the power lost per unit mass (W/kg),

B is the magnetic flux density (T),

d is the thickness of the sheet (m),

f is the frequency (Hz),

ρ is the resistivity of the material ($\Omega \text{ m}$), and

D is the density of the material (kg/m^3).

Fig. 1: The induction heating system: the two susceptors, heated up by eddy currents, impose a thermal gradient to a sample. Susceptors together with sample constitute the mobile set. The coil is represented in dashed lines.

Usually, T_l and T_h cannot be defined as linear functions of P_l and P_h (respectively, the power dissipation of eddy currents in the lower and upper susceptors), mainly because the heat losses of the susceptors are not proportional to their temperatures. In this case, we can only impose and control either T_l or T_h and thus the thermal gradient would not be controlled.

A. A manual generation of a thermal gradient

The schematic diagram (Figure 2) shows two susceptors that are placed on each side of a studied sample. A temperature controller holds a setpoint with a High Frequency (HF) generator from Celes that supplies the induction coil. The eddy currents induced in the susceptors heat them up by joule effect. Thus, the two susceptors generate a thermal gradient across the sample. The temperature of the lower element T_l being regulated with a temperature controller, a variation of T_h and the thermal gradient can be ensured by moving the mobile set along z (see Figure 2). For instance, we used an alumina test sample, 5 mm thick and 10 mm in diameter.

Fig. 2: Schematic diagram of the manual procedure. A temperature controller sets the 4-20 mA current loop with a high frequency (HF: 147 kHz, the frequency generated by our equipment) generator to reach the temperature setpoint T_l . A manual displacement of the mobile set makes it possible to vary T_h and thus ΔT .

After some manual experiments, for a given z , we noticed that T_h and ΔT can be described as linear functions of T_l . Also, for a given T_l , the thermal differential ΔT can be described as a linear function of z . In the next subsections, we will explain why and in which conditions, this modeling can be used in a manual operation or in a computerized automated TGG, how to calibrate the setup and how to operate it

manually, in order to generate a required thermal gradient.

B. Proof of concept

Let us assume that the two susceptors have much higher thermal conductivity than the sample (at least 10 times) and thus there is not a thermal interference between the two susceptors. Let us define two functions F_h and F_l such as:

$$\begin{cases} Th = F_h \cdot Ph + C_1 \\ Tl = F_l \cdot Pl + C_2 \end{cases} \quad (2)$$

F_h and F_l are mainly functions of geometry and the thermal losses of the susceptors. C_1 and C_2 are offsets (constants) originating from the influence of the ambient temperature. Consistently with (1), Ph and Pl are functions of a local peak magnetic field (B_h and B_l , respectively), the other parameters being the same for the two susceptors.

If the thickness of one susceptor is just a few times higher than the other's (but the two circumferences are at least 10 times higher than the two thicknesses), the thermal losses would be similar for the two, since the specific surface doesn't differ much (meaning that $F_h = F_l$). In these conditions and as C_1 , C_2 , Tl , and Th are considered constant, we can write that:

$$\frac{F_h}{F_l} = 1 \rightarrow \frac{Th - C_1}{Tl - C_2} = \frac{Ph}{Pl} = A \quad (3)$$

The constant A will depend mainly on the thicknesses of the two susceptors. Furthermore, if the thickness of the sample is, at least, 10 times smaller than the coil length, meaning that the two susceptors are very close to each other, B_h and B_l would be very similar and thus A would have a value of 1 if the two susceptors have the same thickness and are made with the same material. From equation (3) and posing $C_1 - A \cdot C_2 = T_o$, we obtain:

$$Th = A \cdot Tl + T_o \quad (4)$$

In the following section, we introduce our measurements that are carried out by manual displacements of the mobile set (the two susceptors and the sample) showing that this modeling is possible. Consequently, ΔT can be modeled as:

$$\Delta T = Tl - Th = (1 - A) \cdot Tl - T_o \quad (5)$$

Tl being fixed by the temperature controller, since ΔT can be modeled as a linear function of Tl , we can also assume that, for a fixed position z :

$$\begin{cases} \Delta T = G_l \cdot Tl + m_1 \\ z = G_h \cdot Th + m_2 \end{cases} \quad (6)$$

Where G_h and G_l are mainly functions of geometry and the heat losses of the susceptors. For the same reasons as for the previous case, and with the same conditions, we can write:

$$\frac{G_l}{G_h} = 1 \rightarrow \frac{\Delta T - m_1}{z - m_2} = \frac{Tl}{Th} = k \quad (7)$$

By posing $m = m_1 - m_2 \cdot k$, we obtain:

$$\Delta T = k \cdot z + m \quad (8)$$

It should be noted that a calibration is needed for each type of material used as samples and for any replacement of susceptors.

C. Calibration measurements

A first series of measurements made it possible to demonstrate a good linearity of Th as a function of Tl (with a fixed z position) in stabilized values, as well as good linearity of the differential ΔT as a function of z , at a fixed temperature

Tl . A second series of measurements has been undertaken to study the repetitiveness of the measurements. It confirmed the first series.

a) Variation of the temperature Tl (at $z=0$)

As shown in Figure 3, the measurements allow a linear regression according to (4), with $A=0.8275$ and $T_o=71.31$.

The mobile set is slightly eccentric upwards, with respect to the coil. In this case, Th is lower than or equal to Tl (because the distance to the coil center is larger and the local magnetic field lower). Therefore, we have positive ΔTs , as it is shown in Figure 4.

Fig. 3: Variation of Th as a function of Tl , with constant z . The relationship is linear.

Fig. 4: Variation of ΔT as a function of Tl : linear, in first approximation.

But, ΔT depends also on z and should verify (8). Therefore, in the next section, we vary z , keeping Tl constant at 700°C .

b) Variation of the position z (at $Tl=700^\circ\text{C}$)

Th varies linearly as a function of z (see Figure 5) and Figure 6 shows that ΔT can be modeled linearly (according to equation 8), as a function of z .

The parameter k is a displacement calibration constant. In our case: $k = -3.86^\circ\text{C}/\text{mm}$ and $m = 56.9$ (see Figure 6).

At 700°C , we can therefore have, at most, a gradient of $11^\circ\text{C}/\text{mm}$. This thermal gradient may increase with a more massive upper susceptor, and at higher temperatures.

c) Conditions of the measurements

It is necessary to wait thermal stabilization, a few minutes before taking into account the measurement (2 minutes, in our case). To check if the thermocouples can act as heating elements, we performed a heating cycle with only one thermocouple (without the mobile set): the thermocouple follows the set point (tested up to 150°C). A fast heating of $+25^\circ\text{C}$ is reached in about 3 seconds. Therefore, the thermal

inertia of the thermocouple is low, which means that its temperature adapts to that of the susceptor.

The susceptors have a short response time but a low heat dissipation. For this reason we have chosen a set point rate (SPrr for a Eurotherm controller) at 30°C/min (i.e., 900°C reached in 30 minutes). The controller does not keep the set point in case of a power failure.

Fig. 5: Tl is kept constant in order to study Th as a function of the position z.

Fig. 6: The temperature difference ΔT can be modeled as a function of the position z.

D. Manual control and operation

Let g be the required thermal gradient (°C/mm) and e , the thickness of the studied sample. A manual control is possible as long as the external disturbances are minimized.

a) Manual position adjustment for a required gradient g

To adjust the position, we can calculate $\Delta T = g \cdot e$, then determine Tl with equation (5). Finally, we calculate the position z to be reached in order to get the pair of set points (Tl, ΔT), with equation (8):

$$z = \frac{(\Delta T - m)}{k} \quad (9)$$

b) Typical manual procedure

According to our tests, in this configuration, we can reach a thermal gradient of up to 20 °C/mm and a temperature of up to 1000°C on one of the two faces. The following procedure allows typically the application of a thermal gradient:

- 1- For a given material and thickness, calibrate the system by determining the equations (5) and (8).
- 2- The calibration phase being complete, place a new sample.
- 3- Choose ΔT , i.e. a gradient g given by $g = \Delta T / e$.
- 4- With equation (9), determine and set the position z . The response time of ΔT is longer than the response time of Tl.
- 5- Finally, determine Tl with equation (5) and set it as

setpoint to the temperature controller.

III. A COMPUTER CONTROLLED TGG

The manual procedure has many limitations and makes it difficult to regulate both set points (Th and ΔT) simultaneously to set a gradient. Computer-controlled experimentation can enable the automation of the process. In addition, it has the following advantages:

- a) Do measurements more precisely and save them in a file.
- b) Make the experiments repeatable and reproducible.
- c) Allow an automatic calibration (by a leap of the temperature, then of z). This is very useful if the dimensions of the susceptors are changed or if samples of different sizes, shapes or compositions are used.
- d) Allow a sudden stop of the heating and follow the temperatures Tl and Th (equivalent to a quenching).

A. Configuration in piloted mode with two instructions (Tl, ΔT)

We use a Eurotherm 2404 temperature controller (K type thermocouple) with a serial communication module EIA 232 and a Modbus protocol. The temperature controller can thus be controlled by a PC and a LabView custom application. Figure 7 gives a general scheme of the experimental setup. The real temperature Tl (Process Value) is also read continuously by the PC. The types of thermocouples allowed are: J, K, L, R, B, N, T, S, and PL2. For the measurement of Th, an external data acquisition module (USB) is used (National Instruments: NI cDAQ 9172). A type K thermocouple is used as a sensor. The possible types of thermocouples are: J, K, N, R, S, T, B, and E.

For the control of the temperature differential ΔT , a motorized stage makes it possible to move the mobile set and thus to move along z to reach the desired ΔT . The motorized stage, controlled through a USB port, includes a stepper motor and its controller: Model L490MZ/M from ThorLabs. There are two ways to control this stage, one is absolute, and the other is relative. After some tests, it seems that its absolute control is more robust. Therefore, we chose this mode.

Fig. 7: Overall scheme of the experimental setup. The temperature controller sets Tl through the power of the HF generator while a motorized stage allows the control of ΔT (and Th).

B. Optimization of susceptors

We first tried platinum (Pt) thin layers (by spreading platinum ink on ceramic substrates, then drying). After many tests, we noticed that the platinum layers eventually crack and no longer allow an efficient heating by eddy currents. For this reason, we opted for thin platinum plates that we had at our disposal (currently: 150 μm and about 300 μm thick for the lower and higher susceptors, respectively) of diameter widely greater than that of the sample (our samples are cylindrical pellets). Both Pt plates and PVD (Physical Vapor Deposition) deposited layers could be used to increase thermal contact.

C. Mounting diagram

In Figure 8, the mechanical setup is presented, showing the mobile set under the coil and the possibility of fixing z_0 (initial z) with a preset wheel in z .

Fig. 8: Assembling diagram of the automatic TGG equipment.

In our device, H_s is between 330 mm and 400 mm and can be set with the preset wheel. We fix it once and for all at $H_s=350$ mm. Let H_t be the height at which the axis of the induction coil must be placed, we need a withdrawal margin such as:

$$H_t = H_p + H_s + \text{Withdrawal margin} \\ = 58.5 + 350 + 40 = 448.5 \text{ mm (we fix } H_t=448 \text{ mm).}$$

To have a good mechanical stability, the length of the z -displacement support must be larger than the height of the sample holder and therefore, it is fixed at 325 mm.

D. Control

Since the lower thermocouple is more likely to be in close contact (supporting the weight of the mobile set) than the top one, it is more secure to regulate T_l with the HF generator. If T_h thermocouple is not in contact we risk having an unlimited rise of z . For this reason the maximum movement in the control application is limited to 50 mm, which also corresponds to the maximum stroke of the motorized stage. In order to simplify the control, the rise and the decrease in temperature will be done with the same rate/slope.

Since the heat goes up, if the elements are introduced from the bottom of the coil to the top, we should reach higher

temperature differentials. So we change the configuration, introducing the elements from the bottom of the coil. Thus, in the new configuration, we have :

$$T_h = a \cdot T_l + T_0 \quad (10)$$

$$\Delta T = k' \cdot z + m \quad (11)$$

We want to regulate T_l and ΔT , at the same time. Note that T_0 and m would not have the same values as before. They depend on the initial positions and temperatures.

T_h will be higher than T_l and the roles of T_h and T_l will be reversed. Only the slopes are to be kept (a second series of measurements would determine the new T_0 and m values). If we express T_l as a function of T_h (from equation 4), the slope will be $a = 1/A = 1/0.8275 \approx 1.2$. For the value of k' , approaching from the bottom (z directed upwards), k would keep its value, so finally $k'=k=-3.8611$. Thus, we have a new system of equations:

$$\Delta T = T_h - T_l = (a - 1) \cdot T_l + T_0 \text{ (with } a > 0), \quad (12)$$

$$\Delta T = k \cdot z + m \text{ (} k < 0 \text{ for } z \text{ directed upwards),} \quad (13)$$

where a and k are known, but T_0 and m are to be determined as explained in the next section.

E. Automatic calibration of the TGG

We note that the more massive the higher susceptor is, the faster T_h rises and ΔT is reached. This allows larger ΔT values. The thermal inertia being higher, the increased mass should also yield less fluctuation. To calibrate the TGG completely (example: for a new type of sample), around an operating point, we can determine k , a , m and T_0 by imposing a known leap in z and then a known leap of T_l :

- Calculation of k by a small variation of z :

$$\text{at } z_1: \Delta T_1 = T_{h1} - T_{l1} = k \cdot z_1 + m$$

$$\text{at } z_2: \Delta T_2 = T_{h2} - T_{l2} = k \cdot z_2 + m$$

$$\Delta T_2 - \Delta T_1 = T_{h2} - T_{l2} - T_{h1} + T_{l1} = T_{h2} - T_{h1} = k \cdot (z_2 - z_1)$$

$$\text{from where: } k = (T_{h2} - T_{h1}) / (z_2 - z_1)$$

- Calculation of a by a small variation of T_l :

$$\text{at } T_{l1} = T: T_{h1} = a \cdot T + T_0$$

$$\text{at } T_{l2} = T + T_v: T_{h2} = a \cdot (T + T_v) + T_0$$

$$T_{h2} - T_{h1} = a \cdot T_v,$$

$$\text{from where: } a = (T_{h2} - T_{h1}) / (T_{l2} - T_{l1})$$

- Calculation of m and T_0 to regulate ΔT :

We checked that for different T_l leaps, k is constant and for different z leaps, a is also constant. However, m and T_0 depend on the initial temperature (ambient) and position. We choose a set point (e.g., $z=0$, $T_l=200^\circ\text{C}$). With the equation (10), we calculate $T_0 = T_h - a \cdot T_l$. Then, with the equations (12) and (13), we calculate:

$$m = \Delta T - k \cdot z = (a - 1) \cdot T_l + T_0 - k \cdot z \quad (14)$$

These four parameters can be determined manually, but we also integrated these automatic procedures in our dedicated Labview application. It should be noticed that an optimal velocity of the stage should be chosen (a low value yields fluctuations on ΔT and a high value leads to a permanently turning motor).

We want a small variation $\delta \Delta T$, due to perturbations, to be compensated by a small displacement in δz , hence, after derivation, we obtain from the equation (13), the relation:

$$\delta z = \frac{1}{k} \delta \Delta T \quad (15)$$

This relation is equivalent to a PI (Proportional, Integral) controller which is enough stable in our setup, where the proportional part is null (this is due to the fact that we have a progressively rising or decreasing setpoint).

F. Optimization of the temperature controller parameters

After various tests with our temperature controller, the following PID parameters gave the best results:

$$Pd=6, ti=13, td=2,$$

where, Pd, ti, and td are respectively the proportional, integral and derivative coefficients. For the regulation of ΔT , an acceleration of 0.25 mm/s^2 and a velocity of 0.5 mm/s are the best motorized stage parameters. A new calibration was done at 300°C and gave the following parameters for the TGG:

$$a=1.58 \quad k=-1.06^\circ\text{C/mm} \quad T_o=-95.3^\circ\text{C} \quad \text{and} \quad m=78.4^\circ\text{C}.$$

Note: it is logical that the achievable (maximal) ΔT depends on the chosen TI.

IV. CONTROL SOFTWARE

We designed and built up a dedicated user-friendly LabView application to control the experimental setup. The software environment is as follows: a PC for a development carried out on Windows XP and a LabView license (version 8.6, Full development). The developed application (see Figure 9) saves some values each second (or with a selected period) during an automatic thermal gradient generation with a chosen temperature profile. These values are: Time, Th, TI, ΔT , z and the phase (increase, decrease, dwell) represented by respectively by "M", "D" and "—".

Fig. 9: Global view of the control software (with "Experimentation" tab selected).

The different tabs of the "Gradient" application are: "Parameters", "Experimentation", "Manual Mode", "Reserved" and "Help"). This control software is developed in LabView 8.6 graphical language. In the "Reserved" tab, there is, in particular, the possibility of recalibrating the system (determining a, k, To and m).

One can see the different tabs during the experimentation. Some parameters, such as dwell time, Th and therefore ΔT can be changed throughout the ongoing experiment, if necessary. A certain number of commands and measured values are available in all the tabs (e.g., Th, TI, action on z) to be able to follow the experiment at any time and react as quickly as possible, if necessary.

Figure 10 shows a general view of the equipment, while Figure 11 shows the top views of the coil and the mobile set during experiments at two different temperatures.

Fig. 10: a general view of the experimental setup, with the coil and the mullite support seen in the upper-right corner (in red and white, respectively).

Fig. 11: Photographs during experimentations. Left and right pictures: the higher susceptor and thermocouple can be seen at around 750°C and 800°C , respectively. The susceptor appears white in the right picture. This is due to a wider emission spectrum.

V. RESULTS AND VALIDATION

Since platinum plates are used, cracks can be avoided and higher slopes (temperatures rates) scheduled. Three platinum disks (diameter: 14 mm, thickness: 0.15 mm) were cut in a platinum plate. Two contiguous discs, one on the other, were used as upper (higher) susceptor and one disc on the ceramic support as lower susceptor.

A. Gradient with simulation of a "quench" (alumina sample)

This experiment was done at an early stage of development, where the parameters (To, k, and m) were not well calibrated. Therefore, Th is not rigorously stabilized during the 580°C dwell.

An automatic adjustment of the TI regulator was done and gave the following parameters: Pd=194, ti=16, td=2. Then,

an automatic calibration of the system was done at 250°C and it gave the following parameters: $a=1.21$, $T_0=-40.4^\circ\text{C}$, $k=-0.519^\circ\text{C}/\text{mm}$, $m=13.7^\circ\text{C}$. The regulation in z was carried out with the following motorized stage parameters: acceleration= 0.25 mm/s^2 , velocity= 0.5 mm/s .

An experiment at ($T_h=580^\circ\text{C}$, $T_l=550^\circ\text{C}$, slope= $20^\circ\text{C}/\text{min}$) was carried out on a 5 mm thick alumina sample. It is presented in Figure 12 (started at about 500°C).

Fig. 12: An experiment with a "quenching". Note that, immediately after a quench, T_h becomes lower than T_l because of its higher surface of contact with the air and its low thickness.

Before "quenching", the chosen rate is high ($20^\circ\text{C}/\text{min}$), then the variations around the instructions (setpoints) are important. At $t=4.2\text{ min.}$, the heating was stopped abruptly. T_h ends with a value lower than T_l . This is due to the fact that the lower element has a higher thermal inertia (this was done in early development, when the lower susceptor was thicker).

B. Gradient with an imposed duration (semiconducting oxide ceramic sample)

After adjusting the PID of the T_l regulator and a calibration of the system, an experiment at ($T_h=850^\circ\text{C}$, $T_l=700^\circ\text{C}$, slope: $10^\circ\text{C}/\text{min}$) was conducted on a semiconducting oxide ceramic sample, 2 mm thick and 9 mm in diameter. It is presented in Figure 13 (experiment started at room temperature).

For information, at around $T_l=80^\circ\text{C}$ (and even before) the frequency of the HF generator is stabilized at 145.9 kHz.

Fig. 13: An example of experiment, where it can be seen that for T_h temperatures higher than 500°C , the temperatures and thus the ΔT are very well maintained. T_h , T_l , ΔT , and z are saved during the whole experiment.

VI. CONCLUSIONS

With the current setup, we generated thermal gradients under the following conditions: T_h was raised up to 1000°C with ΔT temperature differentials raised up to 150°C for a 2 mm thick sample (which results in a thermal gradient of $75^\circ\text{C}/\text{mm}$). The samples had a thickness of 2 to 5 mm and low thermal conductivity (alumina: $6.2\text{ W} \cdot \text{m}^{-1} \cdot \text{K}^{-1}$ at 1000°C , oxide ceramic: considered lower than that of alumina).

We are currently using this nondestructive testing equipment to study the ionic migration, previously evidenced in LAMOX oxide-ion conductors (see Lacorre et al. [9], Selmi et al. [10]). The capabilities quoted above are sufficient for our purpose. For other applications, the conditions of use could be modified. These conditions will depend on the materials to be studied (thermal conductivity, sample shape, etc.) and simple adaptations that can be done (e.g., differences in thickness between the two platinum plates).

Most of the possible applications are in research and development laboratories where, for instance, the diffusion of chemical species could be studied. Other studies and characterizations could involve the behavior of materials under fire, the behavior of composite materials and building materials submitted to thermal gradients. The TGG could also submit protection tiles and thermal insulators to known and controlled gradients for aging studies.

A modified version of this TGG could be used whenever it is necessary to create a steady-state heat flux in one or two directions, e.g., for conductivity measurements in a vacuum chamber. According to Zhang et al. [11], the alternating directions, easily carried out with our setup, allows better thermal conductivity measurements. Zawilski et al. [12] stress that for small samples (e.g., in thickness), it is difficult to fix sensors on the sample, thus a global thermal conductance measurement, consistent with our setup, is better suited.

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